



Photovoltaic (PV) Power Variability Modeling and Analysis Approaches

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Joshua S Stein Ph.D.
Photovoltaic and Grid Integration Dept.
Sandia National Laboratories
(Email: jsstein@sandia.gov)

Utility Wind Integration Group: Solar Integration
Portland, OR



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Problem Statement

- Solar integration studies will require **credible** PV and CSP power output estimates for systems that are:
 - diversely sized (kW to MWs)
 - time-synchronous
 - sub-hourly (1-min?)
 - distributed unevenly across a region
- Developing a **valid** model of short-term, dynamic solar resource over a large area is the main challenge.
 - PV output is proportional to spatially averaged irradiance over the plant.



Validation Criteria

- **How to judge irradiance/power model validity?**
 - **Comparison of historical measured irradiance and power to predicted values for same time periods**
 - **Clearness index distribution**
 - **Ramp rate distributions**
 - **Duration and magnitude of changes**
 - **Autocorrelation features**
 - **Spatial correlation features**
 - **More?**
- **How much accuracy is necessary?**
 - **Depends on intended application**
 - **Predicting vs. Forecasting**



Prediction vs. Forecasting

- **Prediction**

- Given low resolution, historical solar estimates (e.g., satellite data), predict 1-min PV plant performance for a fleet of different plants located across a balancing area or region.
- Used for testing build-out scenarios

- **Forecasting**

- Prediction of plant performance into the future.
 - Timing and magnitude of regional weather changes at a point or across a balancing area.
 - Location and velocity of fronts (step changes)
- Used for operations planning



Clearness Index

- PV output is primarily a function of integrated insolation reaching the array.
- Clearness index (CI) removes predictable diurnal and seasonal cycles.

$$CI = E/E_a$$

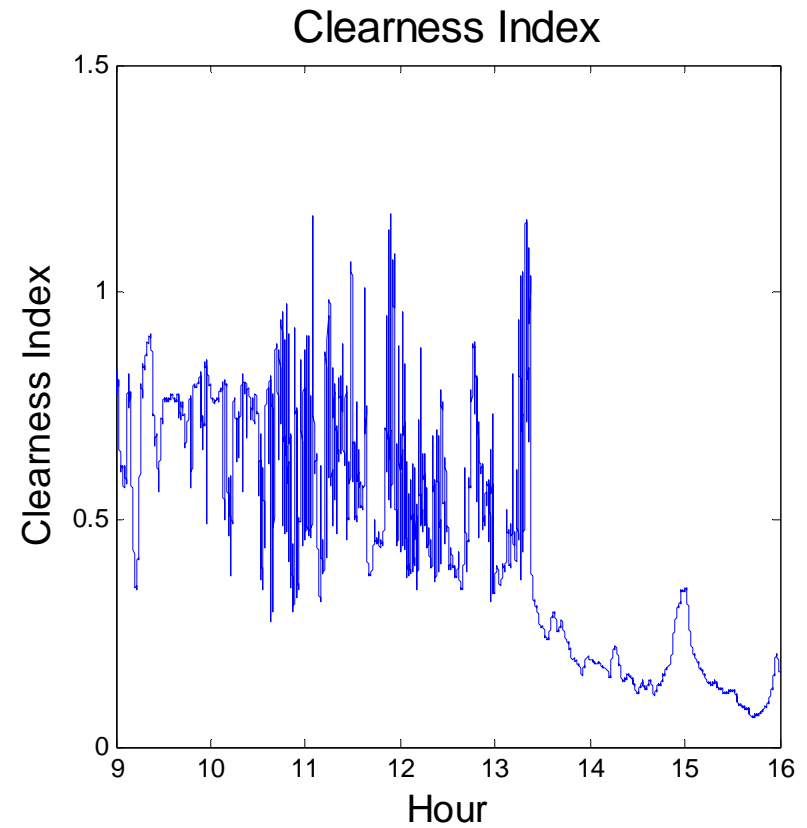
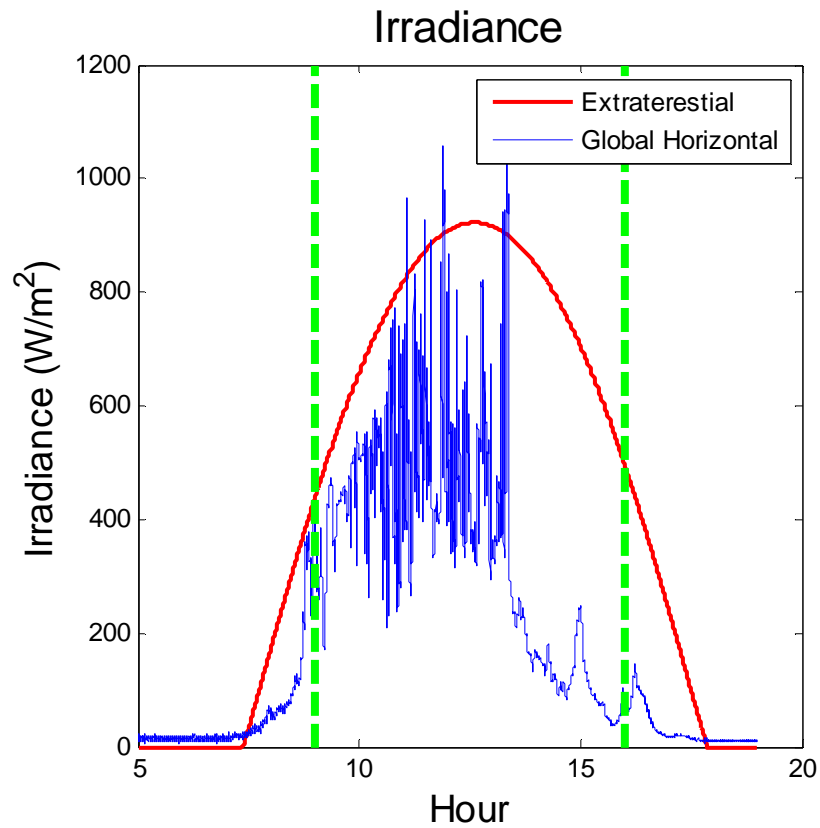
E = global horizontal irradiance [W/m^2]

E_a = extraterrestrial irradiance * cosine(zenith angle)
[W/m^2]

- Clearness index can be converted to irradiance



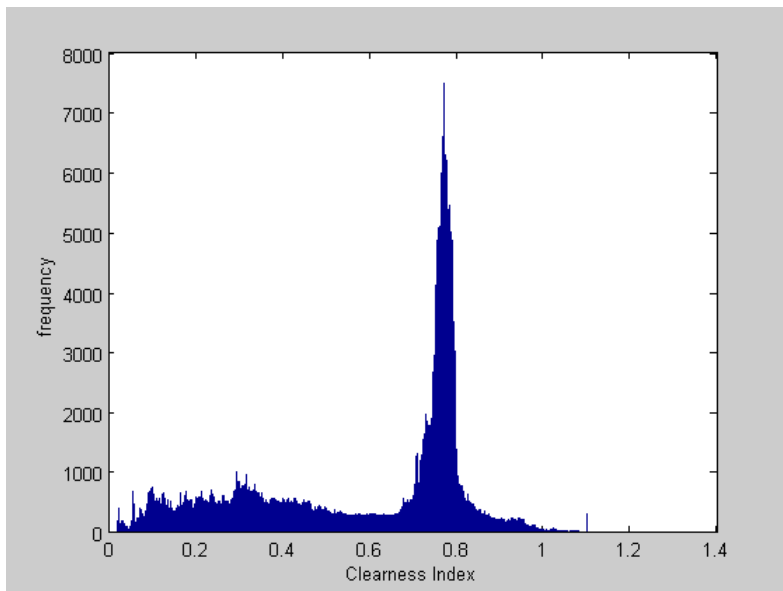
Clearness Index



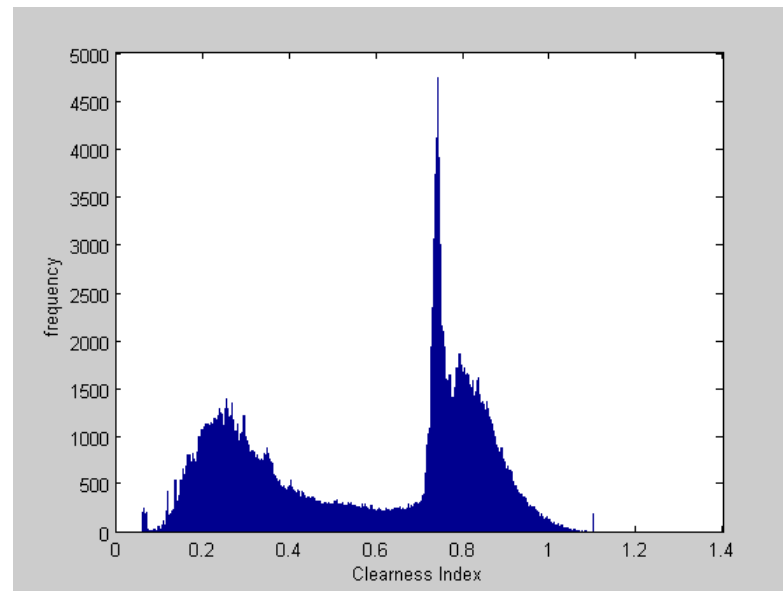


Properties of Clearness Index

- Short time interval measurements of CI exhibit bimodal distributions.
- Valid model should reproduce this pattern.



Florida (1 month)



Hawaii (1 month)



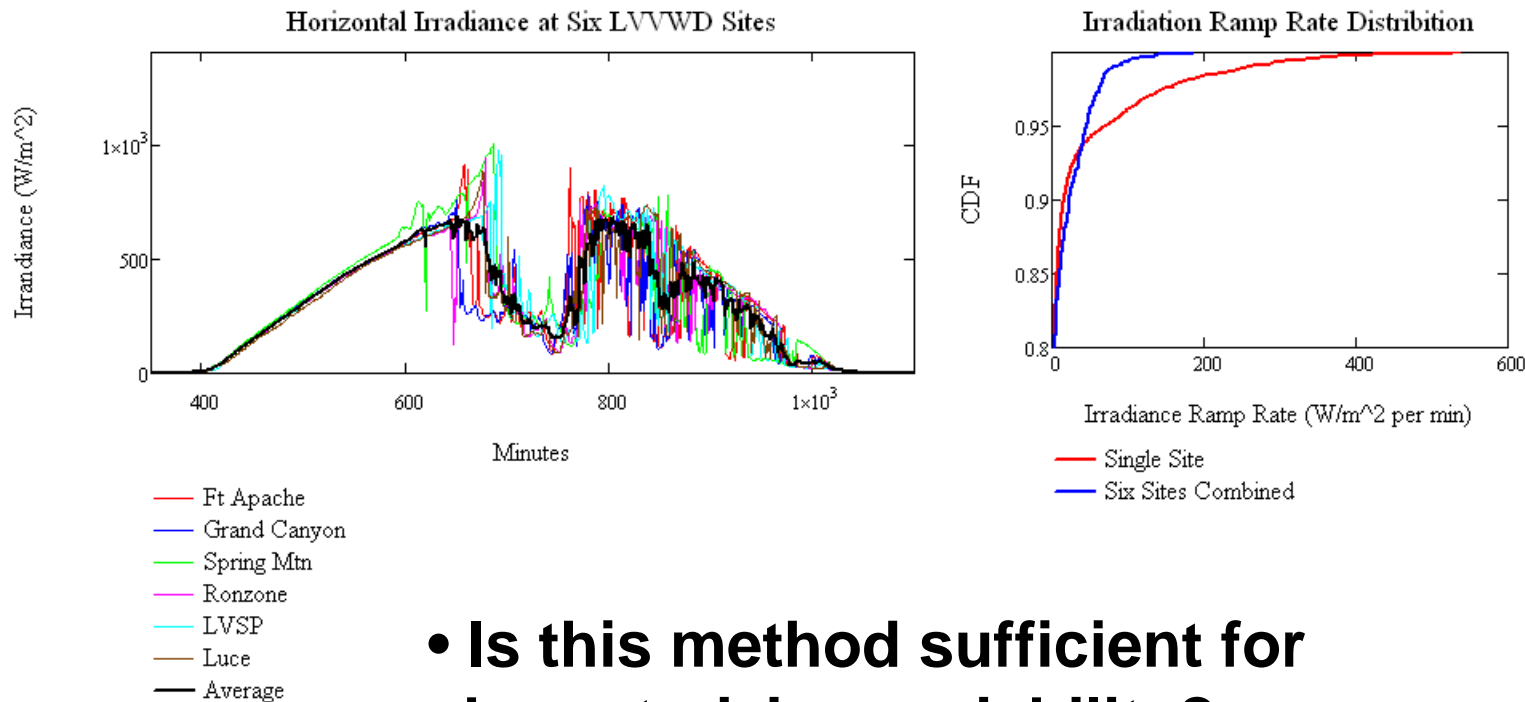
Ramp Rate Distributions (fixed time intervals)

- **Fixed time interval methods examine the distribution of irradiance and power changes ('ramps') over a fixed time interval (e.g., 1-sec, 1-min, 10-min, etc.)**
 - **Analysis of step changes**
 - **Analysis of moving averages**
 - **Regression of data within fixed time windows**
- **This has been a primary focus of PV variability studies.**



Ramp Rate Distributions (fixed time intervals)

- Distribution of fixed time interval ramps provide information about the role of geographic diversity in reducing ramp rates.

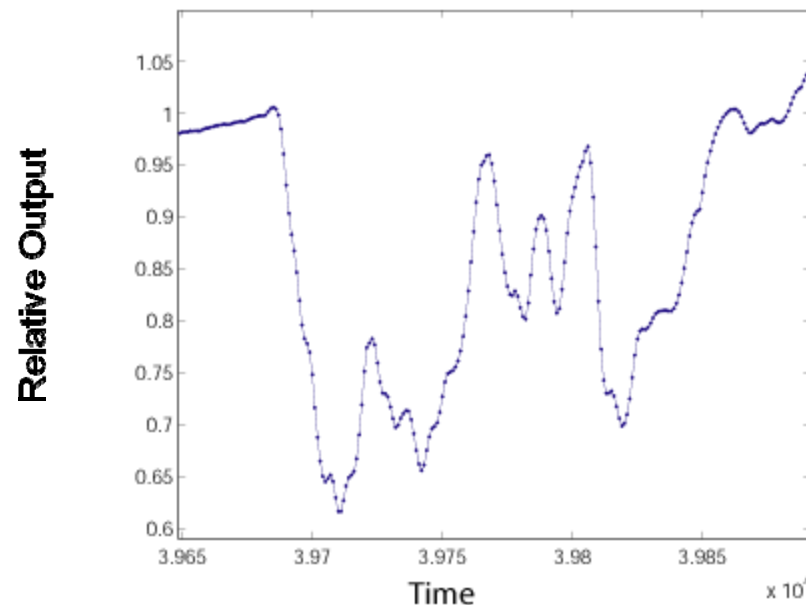


- Is this method sufficient for characterizing variability?



Ramp Events with Flexible Time Intervals

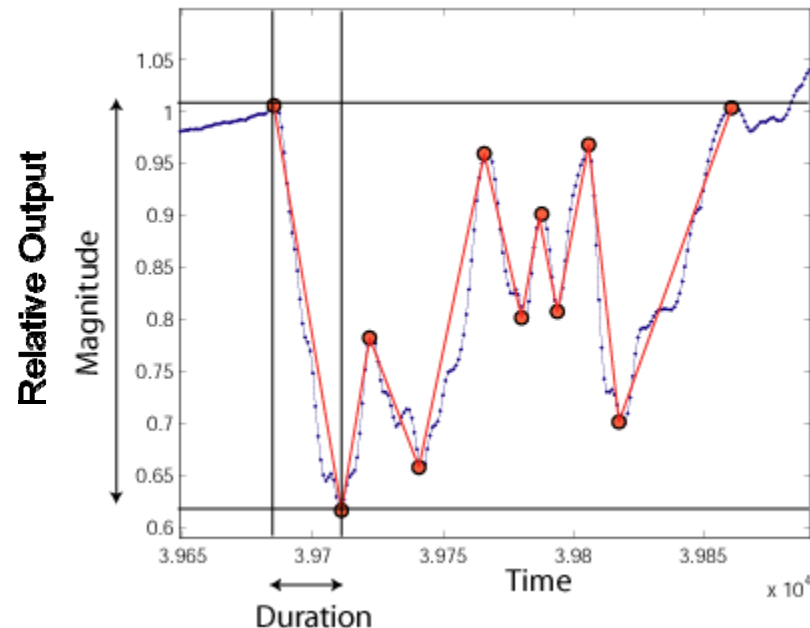
- Utilities want information about frequency of ramp durations and magnitude in order to manage reserves.
 - e.g., 1 min ramp rate might last for 20 minutes.





Ramp Events with Flexible Time Intervals

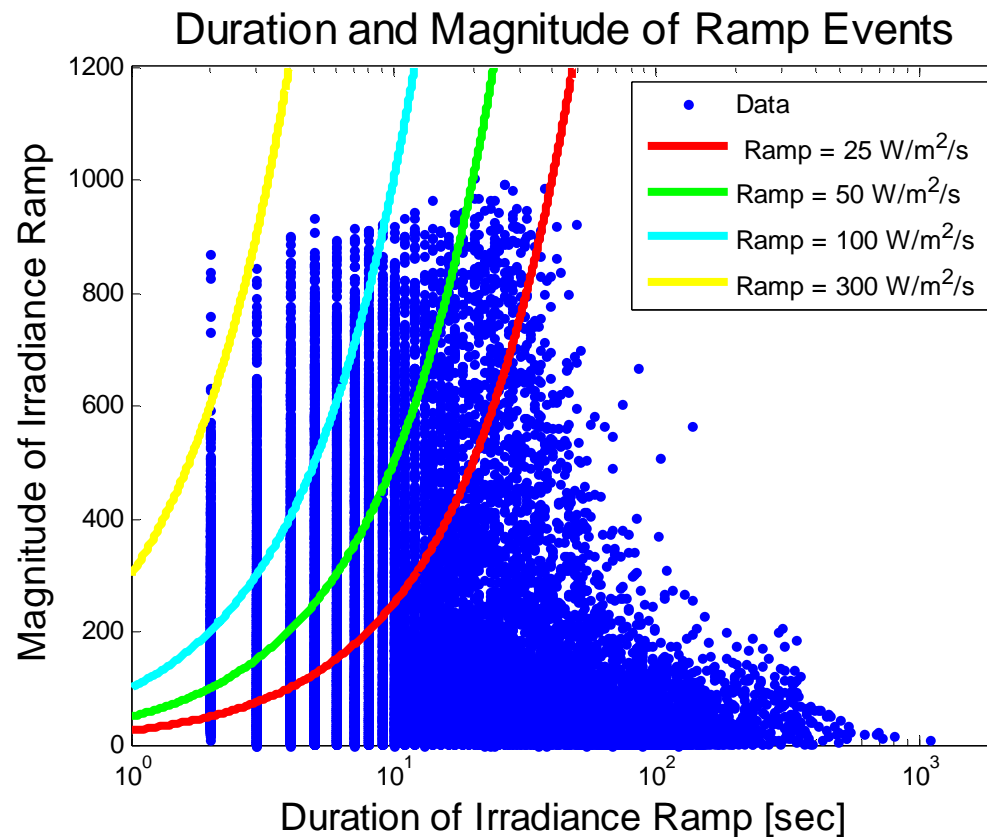
- A piecewise linear approximation calculates 'significant' changes (e.g. Horst and Beichl, 1996 and many others).
 - Results in a reduction of data and an increase in knowledge about the character of the changes.
-
- Ramp events are described by two of three variables:
 - 1) Magnitude (Δp)
 - 2) Duration (Δt)
 - 3) Rate = $\Delta p / \Delta t$





Characterizing Flexible Time Ramp Events

- Bivariate distribution (Duration and Magnitude)
 - 1 month of 1-sec data from Hawaii (~37,000 ramps)





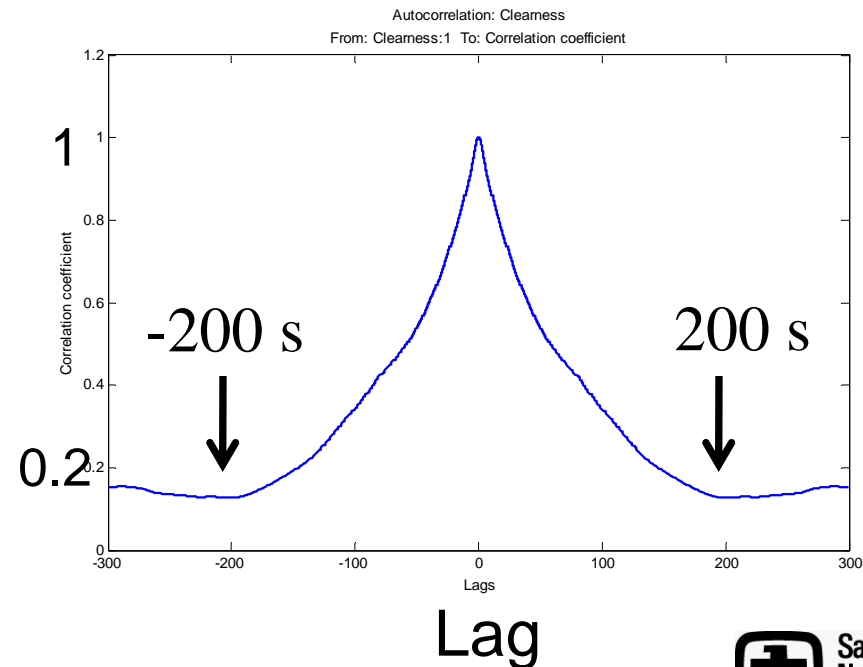
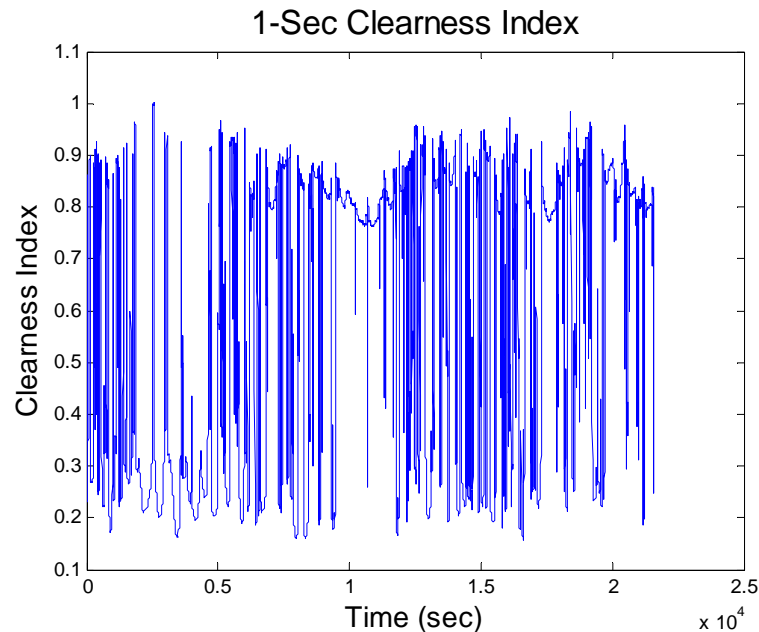
Autocorrelation

- **Clearness indices exhibit autocorrelation features**
 - Shadows extend over large areas and influence output for many time intervals.
 - Autocorrelation plots provide information about the combination of the size and spacing of shadows and the transit speed of the shadows across the ground.
- **Shadow transit speed can be measured (and shadow size and spacing can be inferred)**
 - Aviation weather
 - Irradiance sensor networks



Autocorrelation

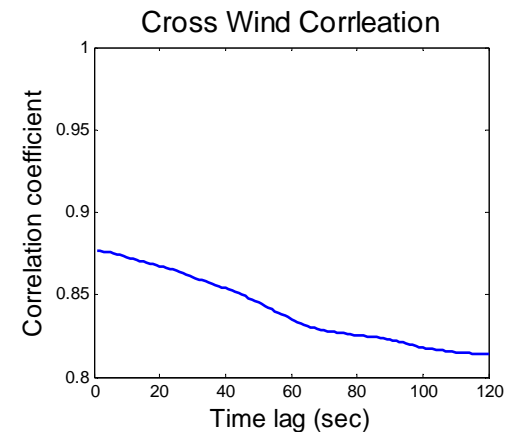
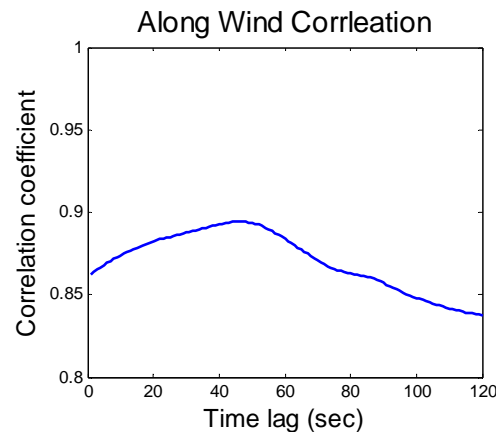
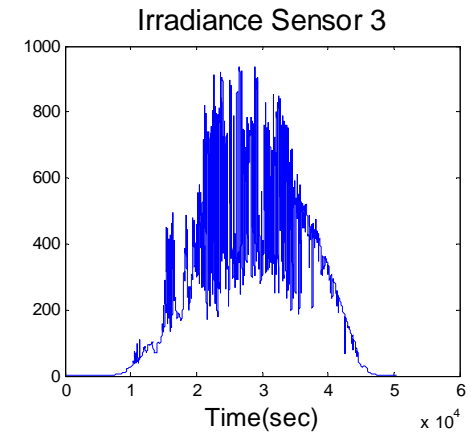
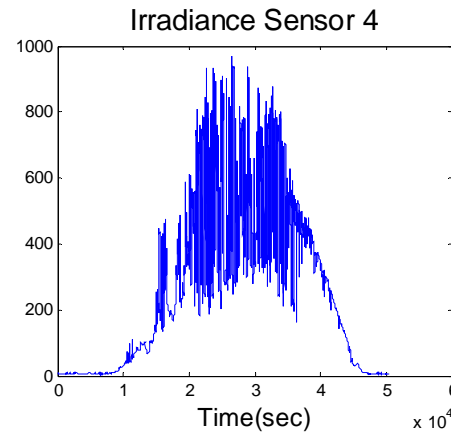
Autocorrelation plot reveals information about characteristic time scale between and inside shadows.





Spatial Correlation Features

- Irradiance (and power) measurements exhibit a spatially and temporally sensitive correlation.
- Cloud patterns can remain relatively static for some time (and distance).
- Autocorrelation features are directional and dependant upon cloud velocity patterns.





Proposed Modeling Approaches

- Plant output is related to a moving average of point irradiance (Longhetto et al., 1989).
 - Assumptions include irradiance is simply time-shifted
 - Falls apart for large or distributed plants
- Hoff and Perez (2009) suggest that relative output variability follows a $1/\sqrt{N}$ relationship.
 - Assumptions include identical PV systems, irradiance variability is the same everywhere, cloud patterns are the same everywhere.
- Autoregressive time series models
 - Glasbey (2000, 2008), Tovar et al. (several papers)
- Cloud (Sky) Simulators
 - Assumes that cloud fields can be predicted from available data (e.g., ground based weather or satellite)



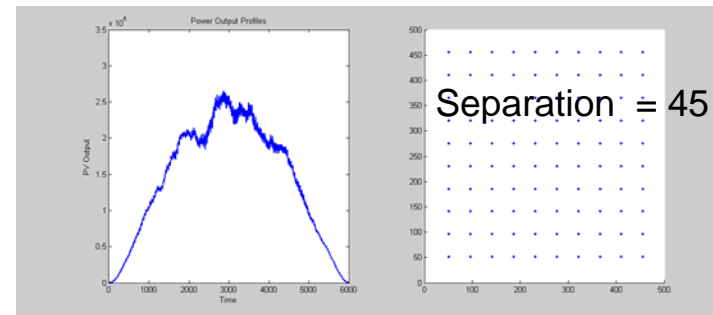
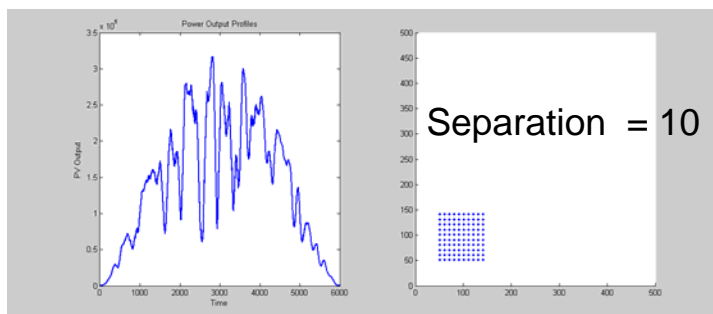
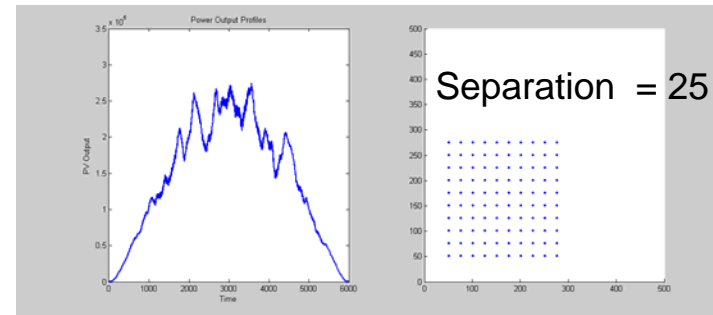
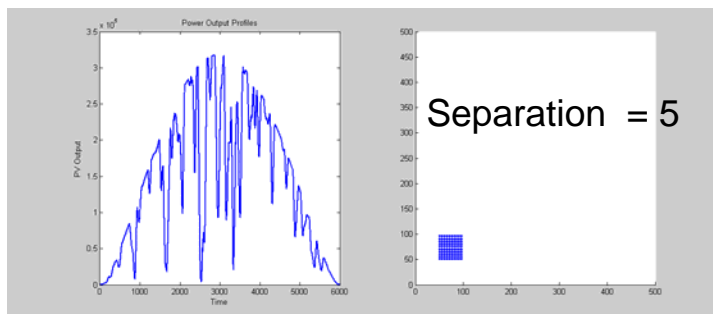
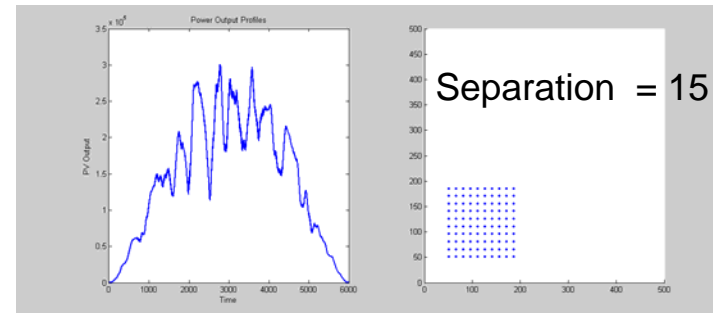
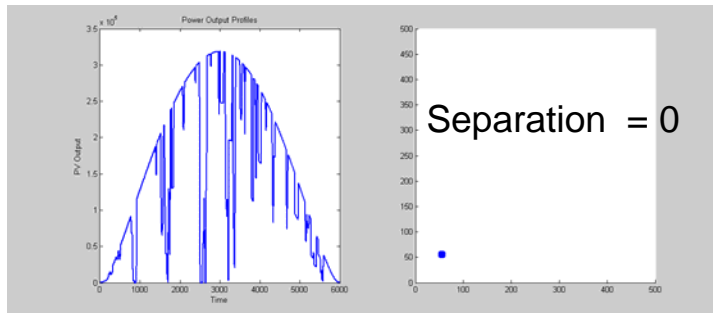
Modeling Effect of Geographic Diversity with Simple Cloud Simulator

- **Synthetic cloud model**
 - Define cloud size range
 - Define cloud transmittance
 - Define cloud coverage
- **(1) Examine different spacing between plants**
 - Fixed capacity PV plant (100 subarrays: 10 x 10)
 - Vary separation of subarrays
 - Examine output variability of fleet for a single synthetic day.
- **(2) Compare small, large, and distributed output**



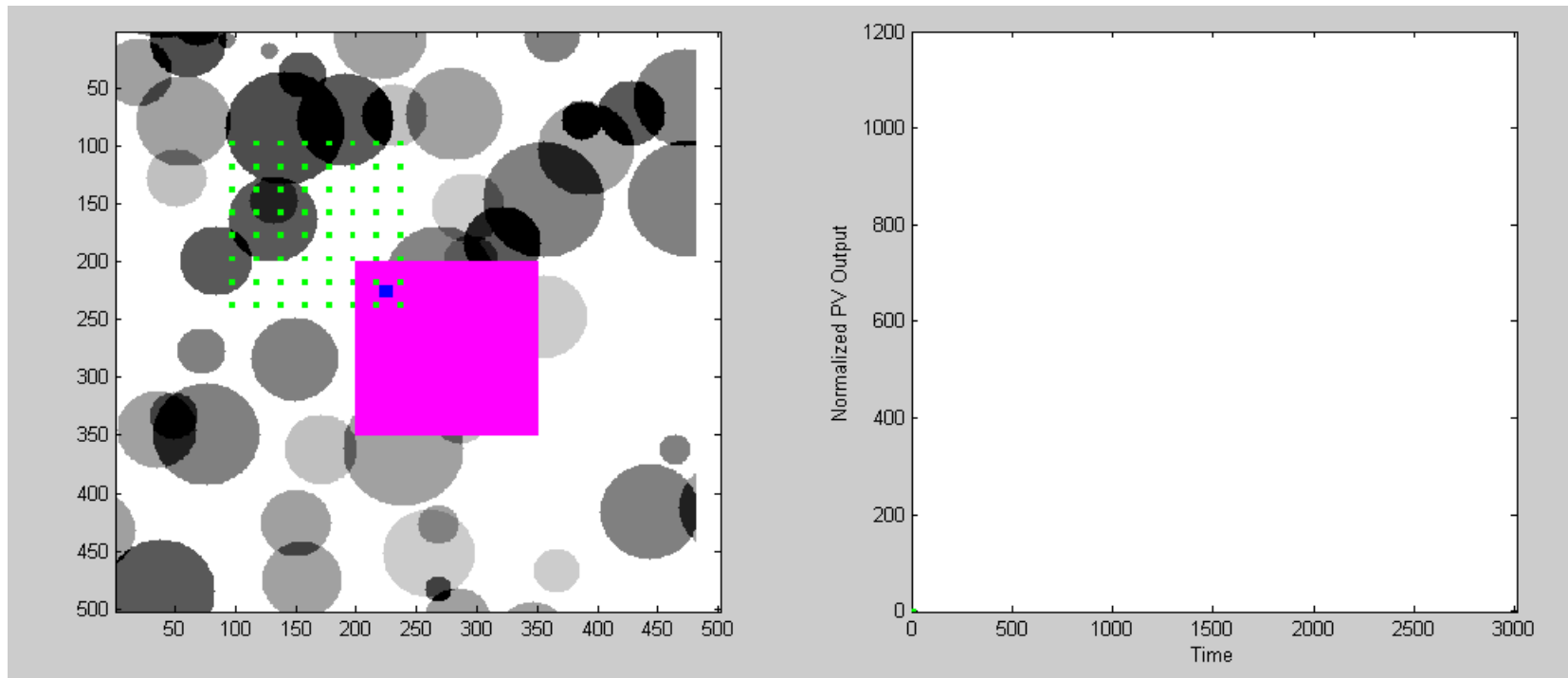


Effect of Geographic Diversity(a)





PVCloudSim Model



Parameters: cloud radius = 10 to 100; transmittance = 0.2 to 0.7, cloud coverage = 0.35
(Clouds can overlap)



Contact Information

Joshua S Stein Ph.D.

Email: jsstein@sandia.gov

Tel: 505-845-0936

Web: <http://photovoltaics.sandia.gov/>